

Questions:

1. **Hash Function (50 Points)** Assume prime $p = 13$ and a generator $g = 7$.

(a) Find two distinct positive integers x and y such that:

$$g^x \pmod p = g^y \pmod p$$

(b) Given the question 1a above, explain why $h(x) = g^x \pmod p$ is not a good hash function.

(c) Does the hash function $h(x) = g^x \pmod p$ satisfy one-wayness, under the condition that p is a large prime?

2. **Digital Certificates (50 Points)**

(a) Why can a public key not just be transmitted through email or be posted on a website?

(b) A certificate does not necessarily have to be signed directly by a CA, there is something called a *certificate chain*. Can you imagine what a certificate chain is?

(c) Who signs the certificate of a CA?