Tutorial 1, Week 2 (March 6)
Due Date: March 20

## Questions:

1. One-Time Pad (20 points):
(a) Alice wants to send the message SECURE to Bob using a one-time pad with the value KTXMLU. What is the ciphertext?
Hint: First convert the letters into numbers (with binary form) using the table below. Note that all letters should have the same binary length.

| A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| Q | R | S | T | U | V | W | X | Y | Z | , | $\cdot$ | $?$ | $!$ | $\%$ | $\#$ |
| 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 |

(b) What is the plaintext you get if you decrypt the ciphertext from 1a with the key XDMBRO?
(c) Assume a key $K$ is used twice for encrypting two different plaintexts $M_{1}$ and $M_{2}$. Show what information about the plaintexts an adversary can gain just by looking at the two cipertexts $C_{1}$ and $C_{2}$.
2. DES(20 points): Consider a simplified DES with only 3 rounds. Suppose that you are given the key $K$ and a ciphertext $\left(L_{3}, R_{3}\right)$. Show how to compute the plaintext ( $L_{0}, R_{0}$ ).

3. 3DES (20 points): Consider 3DES:

$$
C=\mathrm{DES}_{K_{1}}\left(\mathrm{DES}_{K_{2}}^{-1}\left(\operatorname{DES}_{K_{1}}(M)\right)\right)
$$

where $C, M$ are the ciphertext and plaintext, respectively, and $K=\left(K_{1}, K_{2}\right)$ is the key.
(a) How many keys on average do we have to try in a brute force attack?
(b) What's the effect if $K_{1}=K_{2}$ ?
4. Block Cipher Modes (20 points): Suppose that we have a shift cipher with plaintext/message space specified in the table below. In other words, the space has 16 letters.

Suppose that the shift cipher is used as a block cipher which has 4-bit input and 4-bit output with the conversion between the letters and binary strings given in the table below.

Let the key be $k=2$. Encrypt the plaintext $P=$ IAMBOB using CBC mode with $\mathrm{IV}=0010$.

| A | B | C | D | E | F | G | H |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0000 | 0001 | 0010 | 0011 | 0100 | 0101 | 0110 | 0111 |
| I | J | K | L | M | N | O | P |
| 1000 | 1001 | 1010 | 1011 | 1100 | 1101 | 1110 | 1111 |

5. CTR Mode (20 points): Suppose a user with secret key $K$ runs DES with CTR mode to encrypt data. (1) Discuss whether he need to worry that two IV's, say $I V_{1}$ and $I V_{2}$, in two encryptions are too close so that $I V_{2}=I V_{1}+j$ for some $j$. (2) Discuss whether he needs to worry $I V+i$ equals to $I V$ for some large $i$.
Hint: Note that $I V$ is chosen randomly and uniformly.
